NIMCET – 2023

Original Paper

01.	A circle touches the x-axis and also touches the circle with centre (0, 3) and radius 2. The locus of the centre
	of the circle is

- (a) a circle
- (b) an ellipse
- (c) a parabola
- (d) a hyperbola

Sol. (c)

Let C_1 (h,k) be the center of the circle.

Circle touches the x-axis then its radius is $r_1 = k$.

Also circle touches the circle with centre C₂

(0,3) and radius $r_2 = 2$.

$$\therefore |C_1 C_2| = r_1 + r_2$$

$$\Rightarrow \sqrt{(h-0)^2 + (k-3)^2} = |k+2|$$

$$\Rightarrow$$
 h² -10k + 5 = 0

Change h to x and k to y

$$\Rightarrow$$
 $x^2 - 10y + 5 = 0$

It is a parabola.

02. A computer producing factory has only two plants T₁ and T₂. Plant T₁ produces 20% and plant T₂ produces 80% of total computers produced. 7% of computers produced in the factory turn out to be defective. It is known that P (computer turns out to be defective given that it is produced in plant T_1) = 10P (computer turns out to be defective given that it is produced in plant T₂). where P(E) denotes the probability of an event E. A computer produced in the factory is randomly selected and it does not turn out to be defective. Then the probability that it is produced in plant T, is

- (a) $\frac{36}{73}$
- (b) $\frac{47}{79}$ (c) $\frac{78}{93}$
- (d) $\frac{75}{83}$

Sol.

Let x = P (computer turns out to be defective, given that it is produced in plant T_2).

$$\Rightarrow$$
 $x = P\left(\frac{D}{T_2}\right)$ (i)

where, D = Defective computer.

P(computer turns out to be defective given that is produced in plant T_1) = 10x *:* .

i.e.,
$$P\left(\frac{D}{T_1}\right) = 10x$$
(ii)

Also,
$$P(T_1) = \frac{20}{100}$$
 and $P(T_2) = \frac{80}{100}$.

Given, P (defective computer) =
$$\frac{7}{100}$$

i.e.,
$$P(D) = \frac{7}{100}$$

Using law of total probability,

$$P(D) = P(T_1) \cdot P\left(\frac{D}{T_1}\right) + P(T_2) \cdot \left(\frac{D}{T_2}\right)$$

$$\therefore \frac{7}{100} = \left(\frac{20}{100}\right) \cdot 10x + \left(\frac{80}{100}\right) \cdot x$$

$$\Rightarrow 7 = (280) x \Rightarrow x = \frac{1}{40} \qquad \dots (iii)$$

$$\therefore \qquad P\left(\frac{D}{T_2}\right) = \frac{1}{40} \text{ and } P\left(\frac{D}{T_1}\right) = \frac{10}{40}$$

$$\Rightarrow P\left(\frac{\overline{D}}{T_2}\right) = 1 - \frac{1}{40} = \frac{39}{40} \text{ and } P\left(\frac{\overline{D}}{T_1}\right) = \frac{30}{40} \qquad \dots (iv)$$

Using Baye's theorem,

$$P\left(\frac{T_2}{\overline{D}}\right) = \frac{P(T_2) \cdot P\left(\frac{\overline{D}}{T_2}\right)}{P(T_1) \cdot P\left(\frac{\overline{D}}{T_1}\right) + P(T_2) \cdot P\left(\frac{\overline{D}}{T_2}\right)}$$

$$=\frac{\frac{80}{100} \cdot \frac{39}{40}}{\frac{20}{100} \cdot \frac{30}{40} + \frac{80}{100} \cdot \frac{39}{40}} = \frac{78}{93}$$

03. The mean of 5 observation is 5 and their variance is 124. If three of the observations are 1,2 and 6; then the mean deviation from the mean of the data is:

Sol. (

Let the two numbers be x & y.

Given, variance $\sigma^2 = 124$

Mean, $\overline{x} = 5$ and n = 5.

$$\frac{1+2+6+x+y}{5} = 5$$
$$x + y = 16.$$

So, mean deviation =
$$\frac{|1-5|+|2-5|+|6-5|+|x-5|+|y-5|}{5}$$

Now we consider x, y > 5

Mean deviation =
$$\frac{4+3+1+(x+y-10)}{5} = \frac{8+16-10}{5} = \frac{14}{5} = 2.8$$

04.	The perimeter of a Δ angle A is	ABC is 6 times the arith	nmetic mean of the sines	of its angles. If the side a is 1, then the	
Sol.	(a) $\frac{\pi}{6}$	(b) $\frac{\pi}{3}$	(c) $\frac{\pi}{2}$	(d) π	
201	(a) Let the sides of the triangle are a, b, c. It is given that the perimeter of a triangle ABC is 6 times the Arithmetic Mean of the sines of its angles.				

$$\therefore a + b + c = 6 \left(\frac{\sin A + \sin B + \sin C}{3} \right)$$

$$a + b + c = 2(\sin A + \sin B + \sin C)....(1)$$

From the law of sine,

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = k$$

$$\Rightarrow$$
 a = k sin A \Rightarrow b = k sin B \Rightarrow c = k sin C

$$\therefore a + b + c = k \left(\sin A + \sin B + \sin C \right) \dots (2)$$

Hence
$$k = 2 \Rightarrow a = 2 \sin A \Rightarrow 1 = 2 \sin A \Rightarrow \sin A = \frac{1}{2}$$

$$A = \frac{\pi}{6}$$

- **05.** In an examination of nine papers, a candidate has to pass in more papers than the number of papers in which he fails in order to be successful. The number of ways in which he can be unsuccessful is
 - (a) 255
- (b) 256
- (c) 128
- (d) $9 \times 8!$

Sol. (b)

The candidate is unsuccessful if he fails in 9 or 8 or 7 or 6 or 5 papers.

 $\therefore \qquad \text{The number of ways to be unsuccessful} = {}^9C_9 + {}^9C_8 + {}^9C_7 + {}^9C_6 + {}^9C_5$

$$= {}^{9}C_{0} + {}^{9}C_{1} + {}^{9}C_{2} + {}^{9}C_{3} + {}^{9}C_{4} = \frac{1}{2} ({}^{9}C_{0} + {}^{9}C_{1} + \dots + {}^{9}C_{9}) = \frac{1}{2} 2^{9} = 256$$

- **06.** For a group of 100 candidates, the mean and standard deviation of scores were found to be 40 and 15 respectively. Later on, it was found that the scores 25 and 35 were misread as 52 and 53 respectively. Then the corrected mean and standard deviation corresponding to the corrected figures are
 - (a) 39.9, 14.97
- (b) 39.5, 14
- (c) 39.55, 14.97
- (d) 40.19, 15.1

Sol. (c)

$$\overline{x} = 40 = \frac{\sum x_i}{100} \Rightarrow \sum x_i = 4000$$

$$\sum x_i = 4000 - (52 + 53) + (25 + 35) = 3955 \Rightarrow \text{Correct } \overline{x} = 39.55$$

As from given options only (c) option is matched.

Class interval 10-20 20-30 30-40 60-70 70-80 40-50 50-60 **Frequency** 180 f, 34 180 136 50 f,

If the total frequency is 685 & median is 42.6 then the values of f_1 and f_2 are

Sol. (d)

Total frequency = 685

$$580 + f_1 + f_2 = 685$$

$$f_1 + f_2 = 105$$

Median = 42.6 (given) lies in (40-50) interval

Class = 40 - 50.

$$Median = \ell + \frac{\frac{N}{2} - C \cdot f}{f} \times h$$

$$\ell = 40, h = 10$$

$$\mathbf{C} \cdot \mathbf{f} = 214 + \mathbf{f}_1$$

$$42.6 = 40 + \frac{\frac{685}{2} - (214 + f_1)}{180} \times 10$$

$$2.6 \times 18 = 342.5 - 214 - f_1$$

$$f_1 = 81.7 \cong 82$$

$$f_2 = 105 - 82 = 23$$

08. If
$$f(x) = \lim_{x \to 0} \frac{6^x - 3^x - 2^x + 1}{\log_e 9(1 - \cos x)}$$
 is a real number then $\lim_{x \to 0} f(x) = 1$

$$(c) \log_{e} 2$$

$$(d) \log_{a} 3$$

Sol. (c

$$\lim_{x \to 0} \frac{(3^{x} - 1)(2^{x} - 1)}{2\log_{e} 3\left(2\sin^{2} \frac{x}{2}\right)}$$

Using
$$\lim_{x\to 0} \frac{a^x - 1}{x} = \log_e a$$

$$= \frac{1}{4\log_e 3} \lim_{x \to 0} \frac{\left(3^x - 1\right)}{x} \frac{\left(2^x - 1\right)}{x} \frac{4\left(\frac{x^2}{4}\right)}{\sin^2 \frac{x}{2}}$$

$$=\frac{1}{\log_{e} 3}\log_{e} 3 \log_{3} 2 = \log_{e} 2$$

The sum of infinite terms of decreasing GP is equal to the greatest value of the function $f(x) = x^3 + 3x - 9$ in the 09. interval [-2, 3] and difference between the first two terms is f'(0). Then the common ratio of the GP is

(a)
$$-\frac{2}{3}$$

(b)
$$\frac{4}{3}$$

(c)
$$+\frac{2}{3}$$
 (d) $-\frac{4}{3}$

(d)
$$-\frac{4}{3}$$

Sol.

$$f(x) = x^3 + 3x - 9$$
 $x \in [-2, 3]$

Differentiate with respect to x

$$f'(x) = 3x^2 + 3$$

Hence f(x) is strictly increasing function so its greatest value will be at x = 3

$$f(3) = 3^3 + 3 \times 3 - 9 = 27$$

$$\frac{a}{1-r} = 27$$

$$\Rightarrow$$
 a = 27 - 27r

$$\Rightarrow$$
 a + 27r = 27

$$f'(0) = 3$$

Also given a - ar = f'(0)

$$\Rightarrow$$
 a $(1-r) = 3$

$$\Rightarrow 1-r = \frac{3}{a}$$

From eq, 1 and 2 we get

$$a+27\left(1-\frac{3}{a}\right)=27$$

$$a + 27 - \frac{81}{a} = 27$$

$$\Rightarrow$$
 a² = 81 \Rightarrow a = \pm 9

: G.P. is decreasing

$$\therefore$$
 a = 9.

Now,
$$\frac{9}{1-r} = 27 \Rightarrow \frac{1}{3} = 1-r$$

$$r = 1 - \frac{1}{3}$$

$$r = \frac{2}{3}$$

10. The value of
$$\int_{-\pi/3}^{\pi/3} \frac{x \sin x}{\cos^2 x} dx$$
 is

(a)
$$\frac{1}{3}(4\pi+1)$$

(a)
$$\frac{1}{3}(4\pi+1)$$
 (b) $\frac{4\pi}{3} - 2\log\tan\frac{5\pi}{12}$ (c) $\frac{4\pi}{3} + \log\tan\frac{5\pi}{12}$ (d) $\frac{4\pi}{3} - \log\tan\frac{5\pi}{3}$

(d)
$$\frac{4\pi}{3}$$
 - log tan $\frac{5\pi}{3}$

Sol. **(b)**

$$I = 2 \int_{0}^{\pi/3} x \tan x \sec x dx$$
 Using integration by parts

$$I = 2 \left[x \sec x \right]_0^{\pi/3} - 2 \int_0^{\pi/3} \sec x dx$$

$$= 2\left[\frac{\pi}{3} \times 2\right] - 2\left[\ln|\sec x + \tan x\right]_0^{\pi/3}$$

$$= \frac{4\pi}{3} - \left[\ln|2 + \sqrt{3}| \right] = \frac{4\pi}{3} - 2\ln \tan \frac{5\pi}{12}$$

The equation of the tangent at any point of curve $x = a \cos 2t$, $y = 2\sqrt{2}a \sin t$ with m as its slope is 11.

(a)
$$y = mx + a \left(m - \frac{1}{m}\right)$$

(b)
$$y = mx - a\left(m + \frac{1}{m}\right)$$

(c)
$$y = mx + a\left(a + \frac{1}{a}\right)$$

(d)
$$y = amx + a\left(m - \frac{1}{m}\right)$$

Sol.

Eq. of tangent, with slope m.

$$x = a \cos 2t$$

$$y = 2\sqrt{2}a \sin t$$

$$\frac{dx}{dt} = -2a \sin 2t$$

$$\frac{dy}{dt} = 2\sqrt{2}a\cos t$$

$$\frac{dy}{dx} = \frac{dy/dt}{dx/dt} = \frac{2\sqrt{2}a\cos t}{-2a\sin 2t} = \frac{\sqrt{2}\cos t}{-2\sin t\cos t} = \frac{-1}{\sqrt{2}\sin t} = m \text{ given}$$

$$\sin t = \frac{-1}{\sqrt{2}m}$$

$$\sin t = \frac{-1}{\sqrt{2}m} \Rightarrow \boxed{\sin t = \frac{-1}{\sqrt{2}m}}$$

Then

$$x = a \cos 2t$$

$$y = 2\sqrt{2}a \sin t$$

$$= a \left(1 - 2 \sin^2 t \right)$$

$$= a \left(1 - 2\sin^2 t \right) \qquad = 2\sqrt{2}a \times \left(\frac{-1}{\sqrt{2}m} \right)$$

$$= a \left(1 - 2 \times \left(\frac{-1}{\sqrt{2}m} \right)^2 \right) \qquad y = \frac{-2a}{m}$$

$$y = \frac{-2a}{m}$$

$$x = a \left(1 - \frac{1}{m^2} \right)$$

Then Eq. of tangent.

$$y - y_1 = m(x - x_1)$$

$$y + \frac{2a}{m} = m \left(x - a \left(1 - \frac{1}{m^2} \right) \right)$$

$$y + \frac{2a}{m} = mx - am + \frac{a}{m}$$

$$y = mx - a\left(m + \frac{1}{m}\right)$$

 $\textbf{12.} \qquad \text{If } \prod_{i=1}^n tan\left(\alpha_i\right) = 1 \ \, \forall \alpha_i \in \left[0,\frac{\pi}{2}\right] \text{ where } i=1,2,3,.....,n. \text{ Then maximum of value of } \prod_{i=1}^n sin \alpha_i \; .$

- (a) $\frac{1}{2^n}$
- (b) $\frac{1}{2^{n/2}}$
- (c) 1
- (d) None of these

Sol. (b)

 $\sin \alpha_1 \sin \alpha_2 \sin \alpha_3 \dots \sin \alpha_n = \cos \alpha_1 \cos \alpha_2 \dots \cos \alpha_n$

Multiplying both sides by $\sin \alpha_1 \sin \alpha_2 \sin \alpha_3 \dots \sin \alpha_n$

$$\Rightarrow \sin^2 \alpha_1 \sin^2 \alpha_2 \sin^2 \alpha_3 \dots \sin^2 \alpha_n = (\sin \alpha_1 \cos \alpha_1)(\sin \alpha_2 \cos \alpha_2) \dots (\sin \alpha_n \cos \alpha_n)$$

$$\Rightarrow \sin^2 \alpha_1 \sin^2 \alpha_2 \sin^2 \alpha_3 \dots \sin^2 \alpha_n = \frac{1}{2^n} (\sin 2\alpha_1) (\sin 2\alpha_2) \dots (\sin 2\alpha_n)$$

As we know maximum value of $\sin \theta$ is 1

$$\Rightarrow \sin^2 \alpha_1 \sin^2 \alpha_2 \sin^2 \alpha_3 \dots \sin^2 \alpha_n \le \frac{1}{2^n}$$

$$\Rightarrow \sin \alpha_1 \sin \alpha_2 \sin \alpha_3 \dots \sin \alpha_n \le \frac{1}{2^{n/2}}$$

Hence maximum value of $\prod_{i=1}^{n} \sin \alpha_i = \frac{1}{2^{n/2}}$

13. A speaks truth in 60% and B speaks the truth in 50% cases. In what percentage of cases they are likely in contradict each other while narrating some incident is

- (a) 1/2
- (b) 1/4
- (c) 2/3
- (d) 1/3

Sol. (a)

Probability A speaks truth $P(AT) = \frac{60}{100} = \frac{3}{5}$

 \Rightarrow Probability A speaks lie P(AL) = $\frac{40}{100} = \frac{2}{5}$

Probability B speaks truth $P(BT) = \frac{50}{100} = \frac{1}{2}$

$$\Rightarrow$$
 Probability George speaks lie P(BL) = $\frac{50}{100} = \frac{1}{2}$

Probability that they contradict each other stating the same fact = $P(AT \cap BL) + P(AL \cap BT)$

$$=\frac{3}{5}\times\frac{1}{2}+\frac{2}{5}\times\frac{1}{2}=\frac{1}{2}$$

14. If a and b are vector in space, given by
$$a = \frac{\hat{i} - 2\hat{j}}{\sqrt{5}}$$
 and $b = \frac{2\hat{i} + \hat{j} + 3\hat{k}}{\sqrt{14}}$, then the value of $(2a + b) \cdot [(a \times b) \times (a - 2b)]$ is

$$-(2a+b)\cdot[(a-2b)\times(a\times b)]$$

$$= -(2a+b) - \left[\{(a-2b) \cdot b\} \vec{a} - \{(a-2b) \cdot \vec{a}\} \vec{b} \right]$$

$$= (2a+b) \lceil \{(a-2b) \cdot a\} \vec{b} - \{(a-2b) \cdot b\} \vec{a} \rceil$$

$$= \left(2a+b\right) \left\lceil \left\{ \mid a\mid^2 -2b\cdot a \right\} \vec{b} - \left\{ a\cdot b -2\mid b\mid^2 \right\} \vec{a} \; \right\rceil$$

Now,
$$\vec{a} \cdot \vec{b} = \left(\frac{\hat{i} - 2\hat{j}}{\sqrt{5}}\right) \cdot \left(\frac{2\hat{i} + \hat{j} + 3\hat{k}}{\sqrt{14}}\right) = 2 - 2 = 0$$

$$|\vec{a}| = 1, |\hat{b}| = 1$$

$$=(2a+b)\cdot [\{1-0\}\vec{b}-\{0-2\}\vec{a}]$$

$$=(2a+b)\cdot \vec{b}+2\vec{a}$$

$$=(2a+b)\cdot[b+2a]$$

$$= 2a \cdot b + 4 |a|^2 + |b|^2 + 4\vec{a} \cdot \vec{b}$$

$$=0+4+1+0=5$$

15. Let
$$A = 2i + j - 2k$$
 and $B = i + j$, If C is a vector such that $|C - A| = 3$ and the angle between $A \times B$ and C is 30° , then $[(A \times B) \times C] = 3$ then the value of $\vec{A} \cdot \vec{C}$ is equal to

(a)
$$25/8$$

$$\mathbf{A} \times \mathbf{B} = \begin{vmatrix} \hat{\mathbf{i}} & \hat{\mathbf{j}} & \hat{\mathbf{k}} \\ 2 & 1 & -2 \\ 1 & 1 & 0 \end{vmatrix}$$

$$\hat{\mathbf{i}}(2) - \hat{\mathbf{j}}(2) + \hat{\mathbf{k}}(1)$$

$$\hat{i}(2) - \hat{j}(2) + \hat{k}(1)$$

$$A \times B = 2\hat{i} - 2\hat{j} + \hat{k}$$

$$|C - A| = 3$$

$$|\mathbf{C} - \mathbf{A}|^2 = 9$$

17.

Sol.

16.

Sol.

$$\frac{ab + bc + cd}{3} = 9$$

$$\Rightarrow$$
 ab + bc + cd = 27

a, b, c are in HP
$$\Rightarrow$$
 b = $\frac{2ac}{a+c}$ \Rightarrow a + c = $\frac{2ac}{b}$ (i)

b, c, d are in HP
$$\Rightarrow$$
 c = $\frac{2bd}{b+d}$ \Rightarrow b+d = $\frac{2bd}{c}$ (ii)

Multiply (i) and (ii)

$$(a+c)(b+d) = \frac{2ac}{b} \frac{2bd}{c} = 4ad$$

$$(ab+ad+bc+dc) = 4ad$$

$$\Rightarrow$$
 3ad = ab + bc + cd = 27

$$\Rightarrow$$
 ad = 9

Find foci of the equation $x^2 + 2x - 4y^2 + 8y - 7 = 0$ 18.

(a)
$$\left(\sqrt{5}\pm 1,1\right)$$

(a)
$$\left(\sqrt{5} \pm 1, 1\right)$$
 (b) $\left(-1 \pm \sqrt{5}, 1\right)$ (c) $\left(-1\sqrt{5} \pm 1\right)$ (d) $\left(1, -1 \pm \sqrt{5}\right)$

(c)
$$\left(-1\sqrt{5}\pm1\right)$$

(d)
$$(1,-1\pm\sqrt{5})$$

Sol.

$$(x^2+2x+1)-4(y^2-2y)=7+1$$

$$\Rightarrow (x+1)^2 - 4(y-1)^2 = 4$$

$$\Rightarrow \frac{\left(x+1\right)^2}{4} - \frac{\left(y-1\right)^2}{1} = 1$$

Hence center is (-1, 1)

$$b^2 = a^2 (e^2 - 1) \Rightarrow 1 = 4(e^2 - 1)$$

$$\Rightarrow$$
 e = $\frac{\sqrt{5}}{2}$ \Rightarrow ae = $\sqrt{5}$

focii are at a distance ae from center.

Hence focii will be $\left(-1+\sqrt{5},1\right)$ & $\left(-1-\sqrt{5},1\right)$

The locus of the mid-point of all chords of the parabola $y^2 = 4x$ which are drawn through its vertex is 19.

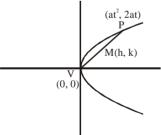
(a)
$$y^2 = 8x$$

(b)
$$v^2 = 2x$$

(c)
$$y^2 + 4y^2 = 16$$
 (d) $x^2 = 2y$

$$(d) x^2 = 2y$$

Sol. **(b)**



Let M be the mid point of VP is (h, k)

$$h = \frac{0 + at^2}{2} \Rightarrow at^2 = 2h \qquad \dots (1)$$

$$k = \frac{0 + 2at}{2} \Rightarrow at = k \Rightarrow t = \frac{k}{a}$$

Put value of t in equation (1) we get $k^2 = 2ah$

Replace $h \rightarrow x$ and $k \rightarrow y$

$$y^2 = 2ax$$

20. If
$$a = \hat{i} - \hat{k}$$
, $b = x\hat{i} + \hat{j} + (1 - x)\hat{k}$ and $c = y\hat{i} + x\hat{j} + (1 + x - y)\hat{k}$, then [**a b c**] depends on

- (a) Neither x nor y
- (b) Only x
- (c) Only y
- (d) Both x and y

Sol. (a)

$$\begin{vmatrix} 1 & 0 & -1 \\ x & 1 & 1-x \\ y & x & 1+x-y \end{vmatrix} = \{(1+x-y)-(x-x^2)\}-0-\{x^2-y\}$$

$$=1+x-y-x+x^2-x^2+y$$

= 1

Depends Neither on x nor, y

21. If
$$\vec{a}$$
, \vec{b} are unit vectors such that $2\vec{a} + \vec{b} = 3$ then which of the following statement is true?

(a) \vec{a} is parallel to \vec{b}

- (b) \vec{a} is perpendicular to \vec{b}
- (c) \vec{a} is perpendicular to $2\vec{a} + \vec{b}$
- (d) \vec{b} is parallel to $2\vec{a} + \vec{b}$

Fundamentally this question is wrong because sum of two vectors can not be equal to scalar. But if we have solve this question.

$$\left|2\vec{a} + \vec{b}\right|^2 = 9$$

$$\Rightarrow 4|\vec{a}|^2 + |\vec{b}|^2 + 4\vec{a} \cdot \vec{b} = 9$$

$$\Rightarrow \vec{a} \cdot \vec{b} = 1$$

$$\Rightarrow |\vec{a}| \cdot |\vec{b}| \cos \theta = 1$$

$$\Rightarrow \cos \theta = 1$$

$$\Rightarrow \theta = 0$$

22.
$$\int f(x)dx = g(x) \text{ then } \int x^5 f(x^3)dx$$

(a)
$$\frac{1}{3}x^3g(x^3) - 3\int x^4g(x^3)dx + c$$

(b)
$$\frac{1}{3}x^3g(x^3) - \int x^2g(x^3)dx + c$$

(c)
$$\frac{1}{3}x^3g(x^3) - \int x^3g(x^3)dx + c$$

(d) None of these

Let
$$x^3 = t$$

$$\Rightarrow 3x^2 dx = dt$$

$$I = \int x^5 f(x^3) dx$$

$$= \int x^2 x^3 f(x^3) dx$$

$$=\frac{1}{3}\int tf(t)dt$$

Using integration by parts

$$I = \frac{1}{3} \left[t \int f(t) dt - \int \left(\frac{dt}{dt} \int f(t) dt \right) dt \right]$$

$$= \frac{1}{3} \left[t g(t) - \int g(t) dt \right]$$

$$= \frac{1}{3} t g(t) - \frac{1}{3} \int g(t) dt$$

$$As x^3 = t \text{ and } dt = 3x^2 dx$$

$$= \frac{1}{3} x^3 g(x^3) - \frac{3}{3} \int x^2 g(x^3) dx$$

$$= \frac{1}{3} x^3 g(x^3) - \int x^2 g(x^3) dx + c$$

23.
$$\lim_{x\to 1} \frac{x^4-1}{x-1} = \lim_{x\to k} \frac{x^3-k^2}{x^2-k^2}$$
 then find k

- (a) 8/3
- (b) 4/3
- (c) 2/3
- (d) 1

Using L'Hospital rule

$$\lim_{x \to 1} \frac{4x^3}{1} = \lim_{x \to k} \frac{3x^2}{2x}$$

$$\Rightarrow 4 = \frac{3}{2}k$$

$$k = \frac{8}{2}$$

24. The graph of function
$$f(x) = \log_e \left(x^3 + \sqrt{x^6 + 1} \right)$$
 is symmetric about:

- (a) x-axis
- (b) y-axis
- (c) origin
- (d) y = x

$$f(x) = \log\left(x^3 + \sqrt{x^6 + 1}\right)$$

$$f(-x) = \log \left[(-x)^3 + \sqrt{(-x)^6 + 1} \right]$$

$$f(-x) = \log \left\lceil \sqrt{x^6 + 1} - x^3 \right\rceil$$

$$= \log \left[\frac{\left(\sqrt{x^6 + 1} - x^3\right)\left(\sqrt{x^6 + 1} + x^3\right)}{\sqrt{x^6 + 1} + x^3} \right]$$

$$= \log \left(\frac{1}{x^3 + \sqrt{x^6 + 1}} \right)$$

$$=\log\left(x^{3}+\sqrt{x^{6}+1}\right)^{-1}$$

$$= -\log\left(x^3 + \sqrt{x^6 + 1}\right)$$

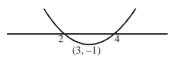
=-f(x) Odd function

We should know that odd functions are symmetrical about origin.

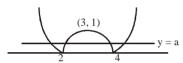
- If the equation $|x^2 6x + 8| = a$ has four real solution then find the value of a? 25.
 - (a) $a \in 0$
- (b) a = 1
- (c) $a \in (0,1)$
- (d) $a \in [1,2]$

Sol. (c)

Let
$$y = x^2 - 6x + 8$$



$$y = |x^2 - 6x + 8|$$



Hence for 4 solutions a must lie between (0, 1).

- Largest value of $\cos^2 \theta 6\sin \theta \cos \theta + 3\sin^2 \theta + 2$ **26.**
 - (a) 4
- (b) 0
- (c) $4 + \sqrt{10}$ (d) $4 \sqrt{10}$

Sol.

$$\cos^2\theta - 6\sin\theta\cos\theta + 3\sin^2\theta + 2$$

$$2\sin^2\theta - 6\sin\theta\cos\theta + 3$$

$$3-3\sin 2\theta + [1-\cos 2\theta]$$

$$=4-\left[3\sin 2\theta+\cos 2\theta\right]$$

$$-\sqrt{10} \le 3\sin 2\theta + \cos 2\theta \le \sqrt{10}$$

For maximum value of given expression

$$3\sin 2\theta + \cos 2\theta$$

It should be minimum. Hence maximum value is $4 + \sqrt{10}$

- **27.** Given to events A and B such that odd in favour A are 2:1 and odd in favour of $A \cup B$ are 3:1. Consistent with this information the smallest and largest value for the probability of event B are given by
 - (a) $\frac{1}{12} \le P(B) \le \frac{3}{4}$ (b) $\frac{1}{3} \le P(B) \le \frac{1}{2}$ (c) $\frac{1}{6} \le P(B) \le \frac{1}{3}$ (d) None of these

Sol. (a)

$$P(A) = \frac{2}{3}$$

$$P(A \cup B) = \frac{3}{4}$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$\frac{3}{4} = \frac{2}{3} + P(B) - P(A \cap B)$$

$$P(A \cap B) = P(B) - \frac{1}{12}$$

$$0 \le P(A \cap B) \le P(A)$$

$$0 \le P(B) - \frac{1}{12} \le \frac{2}{3}$$

$$\frac{1}{12} \le P(B) \le \frac{2}{3} + \frac{1}{12}$$

$$\frac{1}{12} \le P(B) \le \frac{3}{4}$$

- If A and B are square matrices such that $B = -A^{-1}BA$, then $(A + B)^2$ is 28.
 - (a) 0
- (b) $A^2 + B^2$
- (c) $A^2 + 2AB + B^2$ (d) A + B

(b) Sol.

$$\mathbf{B} = -\mathbf{A}^{-1}\mathbf{B}\mathbf{A}$$

$$AB = -(AA^{-1})BA$$

$$AB = -BA$$

$$(A+B)^2 = A^2 + B^2 + AB + BA = A^2 + B^2$$

- 29. A bag contain different kind of balls in which 5 yellow, 4 black & 3 green balls. If 3 balls are drawn at random then find the probability that no black ball is chosen
 - (a) $\frac{14}{55}$
- (b) $\frac{1}{66}$
- (c) $\frac{2}{0}$
- (d) None of these

Sol. (a)

$$5Y + 4B + 3G = 12$$
 balls

Non black ball = 8 balls

P(No black ball is selected) =
$$\frac{{}^{8}C_{3}}{{}^{12}C_{3}} = \frac{8 \times 7 \times 6}{12 \times 11 \times 10} = \frac{14}{55}$$

- 30. Between any two real roots of the equation $e^x \sin x = 1$, the equation $e^x \cos x = -1$ has
 - (a) Atleast one root
- (b) Exactly one root
- (c) No root
- (d) None of these

Sol. (a)

$$e^x \sin x = 1$$

$$f(x) = \sin x - e^{-x}$$

Let it has 2 real roots α, β .

$$f'(x) = \cos x + e^{-x} = 0$$

Using Rolle's theorem

There will be at least one real root of its derivative between α and β .

at least one $c \in (\alpha, \beta)$

$$f'(c) = 0$$

$$e^{-c} + \cos c = 0$$

$$1 + e^{c} \cos c = 0 = g(c)$$

$$g(x) = e^x \cos x + 1$$

$$\alpha < c < b$$

At least one real root of g(x) between two real root of f(x).

31. If f(x) is a polynomial of degree 4, f(n) = n + 1 & f(0) = 25, then find f(5) = ?

(b)
$$20$$

(d) None of these

Sol. (a)

 $f(x) \rightarrow 4$ degree polynomial

Let

$$f(x) = \lambda(x-1)(x-2)(x-3)(x-4) + (x+1)$$

$$f(0) = \lambda(-1)(-2)(-3)(-4) + 1 = 25$$

$$\Rightarrow \lambda = 1$$

$$f(5) = 6 + 24\lambda$$
 Put $\lambda = 1$

$$f(5) = 30.$$

32. The maximum value of $f(x) = (x-1)^2 (x+1)^3$ is equal to $\frac{2^p 3^q}{3125}$ then the ordered pair of (p, q) will be

Sol. (b)

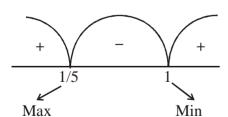
$$f(x) = (x+1)^{2} (x+1)^{3}$$

$$f'(x) = 2(x-1)(x+1)^3 + 3(x+1)^2(x-1)^2$$

$$=(x-1)(x+1)^2 \lceil 2(x+1)+3(x-1) \rceil = 0$$

$$=(x-1)(x+1)^{2}[5x-1]$$

$$x = 1, -1, 1/5$$



$$f\left(\frac{1}{5}\right) = \left(\frac{1}{5} - 1\right)^2 \left(\frac{1}{5} + 1\right)^3 = \left(-\frac{4}{5}\right)^2 \left(\frac{6}{5}\right)^3$$

$$=\frac{16}{5^2}\times\frac{6^3}{5^3}=\frac{2^7\times3^3}{5^5}$$

Hence, p = 7, q = 3.

33. The coefficient of x^{50} in the expression of $(1+x)^{1000} + 2x(1+x)^{999} + 3x^2(1+x)^{998} + \dots + 1001x^{1000}$

(a) ${}^{1005}C_{50}$

(b) $^{1005}C_{48}$

(c) $^{1002}C_{50}$

(d) 1002C₅₁

Sol. (c)

$$Let S = (1+x)^{1000} + 2x(1+x)^{999} + 3x^{2}(1+x)^{998} + + 1000x^{999}(1+x) + 1001x^{1000}$$

Above is A.G.P. of common ratio $r = \frac{x}{1+x}$

$$\left[\frac{x}{(1+x)} \right] S = x (1+x)^{999} + 2x^{2} (1+x)^{998} + \dots + 1000 \cdot x^{1000} + \frac{1001x^{1001}}{1+x}$$

Subtracting,
$$\left(1 - \frac{x}{1+x}\right)S = \left(1+x\right)^{1000} + x\left(1+x\right)^{999} + x^2\left(1+x\right)^{998} + \dots + x^{1000} - \frac{1001x^{1001}}{1+x^{1000}}$$

Or,
$$S = (1+x)^{1001} + x(1+x)^{1000} + x^2(1+x)^{999} + \dots + x^{1000}(1+x) - 1001x^{1001}$$

$$=\frac{\left(1+x\right)^{1001}\left[1-\left(x-\left(1+x\right)\right)^{1001}\right]}{1-x}-1001x^{1001}$$

Sum G.P.
$$(1+x)^{1002} \left[1 - \left(\frac{x}{(1+x)} \right)^{1001} \right] - 1001x^{1001}$$

$$= (1+x)^{1002} - x^{1001} (1+x) - 1001x^{1001}$$

$$= (1+x)^{1002} - x^{1002} - 1002x^{1001} \dots (i)$$

Now the coefficients of x⁵⁰ on the R.H.S. of (i)

$$= {}^{1002}C_{50}$$

34. If $x_k = \cos\left(\frac{2\pi k}{n}\right) + i\sin\left(\frac{2\pi k}{n}\right)$, then $\sum_{k=1}^{n} (x_k) = ?$

(a) 1

(b) -1

(c) 0

(d) None of these

Sol. (c)

We should know that $\cos \theta + i \sin \theta = e^{i\theta}$

$$X_{k} = \frac{\cos 2\pi k}{n} + \frac{i \sin 2\pi k}{n} = e^{i\frac{2k\pi}{n}}$$

$$\sum_{k=1}^{n} X_{k} = \sum_{k=1}^{n} e^{\frac{i^{2k\pi}}{n}} = e^{\frac{i^{2\pi}}{n}} + e^{\frac{i^{4\pi}}{n}} + e^{\frac{i^{6\pi}}{n}} + \dots + e^{\frac{i^{2n\pi}}{n}}$$

Let
$$e^{i\frac{2\pi}{n}} = \alpha$$

Hence this series = $\alpha + \alpha^2 + \alpha^3 + \dots + \alpha^n = \frac{\alpha(1 - \alpha^n)}{1 - \alpha}$

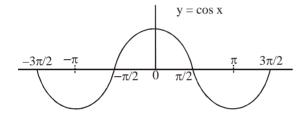
$$=\frac{e^{i\frac{2\pi n}{n}}\left(1-e^{\left(\frac{i2\pi}{n}\right)n}\right)}{1-e^{\frac{i2\pi}{n}}}$$

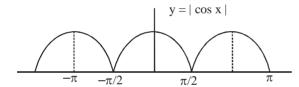
$$\left[e^{i2\pi} = \cos 2\pi + i\sin 2\pi = 1\right]$$

$$= \frac{e^{i\frac{2\pi n}{n}} \left(1 - e^{i2\pi}\right)}{1 - e^{\frac{i2\pi}{n}}} = 0$$

- 35. Number of point of which f(x) is not differentiable $f(x) = |\cos x| + 3 in [-\pi, \pi]$
 - (a) 2
- (b) 3
- (c) 4
- (d) None of these

Sol. (a)





It is not differentiable at two points (We should know the function is not differentiable where there is sharp turns).

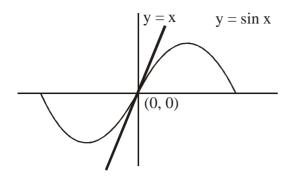
 $y = |\cos x| + 3$ It is not differentiable at $x = \frac{-\pi}{2}, \frac{-\pi}{2}$

- 36. If n_1 and n_2 are the number of real valued solutions $x = |\sin^{-1} x| & x = \sin(x)$ respectively, then the value of $n_2 n_1$ is
 - (a) 1
- (b) 0
- (c)2
- (d)3

Sol. (a)

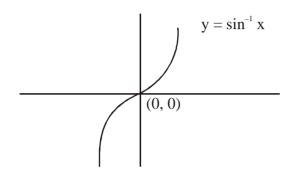
 $x = \sin x$

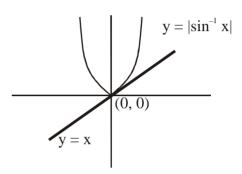
We should know that $\sin x < x < \tan x$ when $x \in \left(0, \frac{\pi}{2}\right)$



Hence $n_2 = 1$ (It has only one solution that (0, 0))

We should know that graph of $f^{-1}(x)$ is mirror image of f(x) with respect to y = x as a mirror.





Number of solutions $n_1 = 1$ (only (0, 0) is the solution of this equation) of eq. $x = |\sin^{-1} x|$ Hence $n_2 - n_1 = 0$

37. Let a, b, c, d be no zero numbers. If the point of intersection of the line 4ax + 2ay + c = 0 & 5bx + 2by + d = 0lies in the fourth quadrant and is equidistance from the two are then

(a)
$$a + b + c + d = 0$$
 (b) $ad - bc = 0$

(b)
$$ad - bc = 0$$

(c)
$$3bc - 2ad = 0$$

(d)
$$3bc + 2ad = 0$$

Sol.

If it lies in the fourth quadrant, we get (x, -x)

2ax + c = 0 and 3bx + d = 0

$$\frac{c}{2a} = \frac{d}{3b}$$

$$3bc - 2ad = 0$$

The negation of $\sim S \vee (\sim R \wedge S)$ is equivalent to 38.

(a)
$$S \lor (R \lor -S)$$
 (b) $S \land \sim R$

(b)
$$S \land \sim R$$

(c)
$$S \wedge R$$

(d)
$$S \wedge (R \wedge \sim S)$$

Sol.

$$\sim (\sim S \vee (\sim R \wedge S))$$

$$= S \wedge (R \vee \sim S)$$

$$= S \cdot (R + \overline{S}) = S \cdot R + S \cdot \overline{S}$$

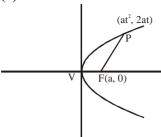
$$=S\cap R+S\cap \overline{S}=S\cdot R+\varphi$$

$$=(S\cap R)\cup \phi=S\cap R$$

A point P in the first quadrant, lies on $y^2 = 4ax$, a > 0, and keeps a distance of 5a units from its focus. Which of **39.** the following points lies on the locus of P?

(d)(2,0)

Sol. (b)



FP = 5a

$$a + at^2 = 5a$$

$$1 + t^2 = 5$$

$$t^2 = 4$$

$$t = \pm 2$$

$$t > 0 \implies t = 2$$

Hence $P \equiv (4a, 4a)$

From given options only (1, 1) satisfy P.

40. If $\int x \sin x \sec^3 x dx = \frac{1}{2} \left[f(x) \sec^2 x + g(x) \left(\frac{\tan x}{x} \right) \right] + c$ then which of the following is true

(a)
$$f(x) - g(x) = 0$$

(b)
$$f(x) \cdot g(x) = 0$$

$$(c) f(x) + g(x) = 0$$

(d)
$$f(x) + g(x) = 1$$

Sol. (c)

 $\int x \sin x \sec^3 x dx = \int x \tan x \sec^2 x dx$ Using integration by part

 $= \left[x \int \sec^2 x \tan x dx \right] - \int \left(\frac{dx}{dx} \int \sec^2 x \tan x dx \right) dx$

$$= \left[x \frac{\tan^2 x}{2} \right] - \int \frac{\tan^2 x}{2} dx$$

$$= \frac{1}{2} \left[x \tan^2 x - \int (\sec^2 x - 1) dx \right]$$

$$= \frac{1}{2} \left[x \tan^2 x - \tan x + x \right] + c$$

$$= \frac{1}{2} \left[x \left(1 + \tan^2 x \right) - \tan x \right] + c$$

$$= \frac{1}{2} \left[x \sec^2 x - \tan x \right] + c$$

$$= \frac{1}{2} \left[f(x) \sec^2 x + g(x) \left(\frac{\tan x}{x} \right) \right] + c$$

Hence, f(x) = x : g(x) = -x

Hence f(x) + g(x) = 0

41. $\theta = \cos^{-1}\left(\frac{3}{\sqrt{20}}\right)$ is the angle between $\vec{a} = \hat{i} - 2x\hat{j} + 2y\hat{k} \& \vec{b} = x\hat{i} + \hat{j} + y\hat{k}$ then possible values at (x, y) that

lie on the locus

Sol. (a)

$$\vec{a} = \hat{i} - 2x\hat{j} + 2y\hat{k} \& \vec{b} = x\hat{i} + \hat{j} + y\hat{k}$$

$$\cos \theta = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}||\vec{b}|} = \cos \cos^{-1} \left(\frac{3}{\sqrt{20}}\right) = \frac{3}{\sqrt{20}}$$

$$\frac{3}{\sqrt{20}} = \frac{x - 2x + 2y^2}{\sqrt{1 + 4x^2 + 4y^2}\sqrt{x^2 + 1 + y^2}}$$

$$\Rightarrow 3\sqrt{1+4x^2+4y^2}\sqrt{x^2+1+y^2} = \sqrt{20} \left[2y^2 - x \right]$$

From Given options (0, 1) satisfy given equations.

42. Let R be reflexive relation on the finite set a having 10 elements and if m is the number of ordered pair in R, then

(a)
$$m \ge 10$$

(b)
$$m = 100$$

(c)
$$m = 10$$

(d)
$$m \le 10$$

Sol. (a)

Given R has m order pairs.

Since R is reflexive relation on A, therefore $(a, a) \in R \forall a \in A$.

Then the minimum no. of ordered pairs in R is 10.

Therefore $m \ge 10$

43. If $|x-6| = |x^2 - 4x| - |x^2 - 5x + 6|$, where x is a real variable

(a)
$$x = (2, 5)$$

(b)
$$x \in [2,3] \cup [6,\infty)$$
 (c) $R - [2,6]$

(d) None of these

Sol. (b

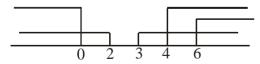
$$|x-6| = |x^2-4| + |(x-3)(x-2)|$$

Its one solution is

$$x(x-4) \ge 0 \& x^2 - 5x + 6 \ge 0$$

And $x \ge 6$

$$x \le 0 \text{ or } x \ge 4$$
 $x \le 2 \& x \ge 3$

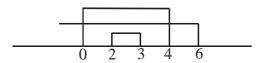


Its intersection $x \ge 6 \Rightarrow x \in [6, \infty)$

Its second solution $x(x-4) \le 0$ & $x^2 - 5x + 6 \le 0$

$$0 \le x \le 4$$
 & $2 \le x \le 3$ & $x < 6$

And $x \le 6$



Its intersection is $2 \le x \le 3 \Rightarrow x \in [2,3]$

Union of both solutions is $x \in [2,3] \cup [6,\infty)$

44. The range of values of θ in the interval $(0,\pi)$ such that the points (3,2) and $(\cos\theta,\sin\theta)$ lie on the same sides of the line x + y - 1 = 0, is

(a) $\left(0, \frac{3\pi}{4}\right)$ (b) $\left(0, \frac{\pi}{2}\right)$ (c) $\left(0, \frac{\pi}{3}\right)$

Sol. **(b)**

$$L: x + y - 1 = 0$$

As (3,2) & $(\cos \theta, \sin \theta)$ lies on same side of line

$$L:(3,2)3+2-1=4>0$$

So, L: $(\cos \theta, \sin \theta) = \sin \theta + \cos \theta - 1 > 0$

$$\Rightarrow \sqrt{2} \left[\frac{1}{\sqrt{2}} \cos \theta + \frac{1}{\sqrt{2}} \sin \theta \right] > 1$$

$$\sin\left(\theta + \frac{\pi}{4}\right) > \frac{1}{\sqrt{2}}$$

$$\Rightarrow \frac{\pi}{4} < \theta + \frac{\pi}{4} < \frac{3\pi}{4}$$

$$\Rightarrow 0 < \theta < \frac{\pi}{2}$$

Which of the following number is the coefficient of x^{100} in the expansion of $\log_e\left(\frac{1+x}{1+x^2}\right)$, |x|<1? **45.**

(a) 0.01

- (b) 0.02
- (c) -0.03
- (d) -0.01

Sol.

$$\log_{e}(1+x) = x - \frac{x^{2}}{2} + \frac{x^{3}}{3} - \frac{x^{4}}{4} + \frac{x^{5}}{5} - \dots - \frac{x^{100}}{100} + \dots$$

$$\ln\left(1+x^2\right) = x^2 - \frac{x^4}{2} + \frac{x^6}{3} - \frac{x^8}{4} + \dots - \frac{\left(x^2\right)^{50}}{50}$$

Coefficient of
$$x^{100}$$
 in $ln\left(\frac{1+x}{1+x^2}\right)$

Coefficient of x^{100} in $\ln(1+x) - \ln(1+x^2)$

$$=-\frac{1}{100}+\frac{1}{50}=0.01$$

A real valued function f is defined as $f(x) = \begin{cases} -1 & -2 \le x \le 0 \\ x - 1 & 0 \le x \le 2 \end{cases}$. Which of the following statement is FALSE? 46.

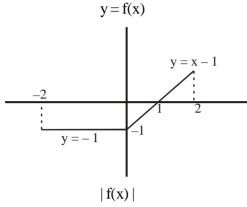
(a) f(|x|) = |x| - 1, if $0 \le x \le 1$

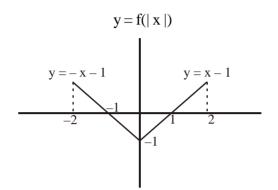
(b) |f(x)| = x - 1, if $1 \le x \le 2$

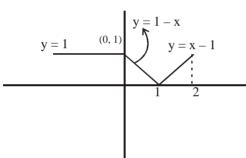
(c) f(|x|) + |f(x)| = 1, if $0 \le x \le 1$ (d) f(|x|) - |f(x)| = 0, if $1 \le x \le 2$

Sol. (c)

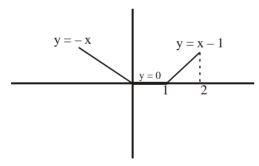
Graphical solution:







Add these two graphs y = |f(x)| + f(|x|)

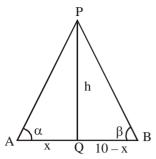


From given graphs we can find that statement (c) is false.

47. A line segment AB of length 10 meters is passing through the foot of the perpendicular of a pillar, which is standing at right angle to the ground. Tip of the pillar subtends angles tan⁻¹ 3 and tan⁻¹ 2 at A and B respectively. Which of the following choice represents the height of the pillar?

- (a) 10 meter
- (b) 8 meter
- (c) 12 meter
- (d) 15 meter

Sol. **(c)**



Let $\alpha = \tan^{-1} 3 \Rightarrow \tan \alpha = 3$ and $\beta = \tan^{-1} 2 \Rightarrow \tan \beta = 2$

In AAPO

$$\tan \alpha = \frac{h}{x} = 3 \Rightarrow x = \frac{h}{3}$$

In ΔBPQ

$$\tan \beta = \frac{h}{10 - x} = 2 \Rightarrow h = 20 - 2x$$

$$\Rightarrow$$
 h = 20 - 2h/3

$$\Rightarrow$$
 h = 12

- 48. If a vector having magnitude of 5 units, makes equal angle with each of the three mutually perpendicular axes, then the sum of the magnitude of the projections on each of the axis is
 - (a) 15/3 unit
- (b) $5\sqrt{3}$ unit (c) $\frac{15\sqrt{3}}{2}$ units (d) None of these

Sol. **(b)**

$$|\vec{v}| = 5$$

As \vec{v} makes equal angle with all the three axis

$$\vec{v} = x\hat{i} + x\hat{j} + x\hat{k}$$

$$|\vec{v}| = \sqrt{3}x = 5$$

$$x = \frac{5}{\sqrt{3}}$$

Sum of component on x, y, z axis

$$x + x + x = 3\left(\frac{5}{\sqrt{3}}\right) = 5\sqrt{3}$$
.

- 49. Bag I contains 3 red, 4 black and 3 white balls and Bag II contains 2 red, 5 black and 2 white balls. One balls is transferred from Bag I to Bag II and then a ball is drawn from Bag II. The ball so drawn is found to be black in colour. Then the probability, that the transferred is red, is:
 - (a) 4/9
- (b) 5/18
- (c) 1/6
- (d) 3/10

Sol. **(b)**

2W

A: Drawn ball from boy II is black

B: Red ball transferred

$$P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)}$$

$$=\frac{\frac{3}{9} \times \frac{5}{10}}{\frac{3}{9} \times \frac{5}{10} + \frac{4}{9} \times \frac{6}{10} + \frac{3}{9} \times \frac{5}{100}} = \frac{15}{15 + 24 + 15} = \frac{15}{54} = \frac{5}{18}$$

50. Let $f(x) = \frac{(x^2 - 1)}{(|x| - 1)}$. Then the value of $\lim_{x \to -1} f(x)$ is

- (a) -1
- (b) 1
- (c) 2
- (c)3

Sol. (c)

$$\lim_{x \to -1} \frac{x^2 - 1}{-(x+1)} = \frac{(x-1)(x+1)}{-(x+1)} = 2$$

Reasoning

- **51.** Complete the series: 3, 10, 24, 45, 73,
 - (a) 69
- (b) 91
- (c) 108
- (d) 121

Ans. (c)

- **52.** Pointing towards a person in the photograph, Anjali said, "He is the only son of the father of my sister's brother". How is that person related to Anjali?
 - (a) father
- (b) mother
- (c) cousing
- (d) None of these

Ans. (d)

- **53.** Book: Publisher:: Film:?
 - (a) Director
- (b) Producer
- (c) Editor
- (d) Writer

Ans. (b)

- **54.** A sum of money distributed among four person P, Q, R, S in ratio 2:5:4:3. If Q get Rs. 2000 more than S, then what will be the total amount
 - (a) 18000
- (b) 16000
- (c) 14000
- (d) 15000

Ans. (c

- P, Q, R, S, T, U, V, W are sitting around a table in the same order, for group discussion at equal distances. Their position are clockwise. If V sit in north, then what will be the position of 'S'
 - (a) East
- (b) South
- (c) South East
- (d) South West

Ans. (d)

- **56.** If yellow is called white, white is called black, black is called green, green is called pink, pink is called blue and blue is called water, what is the colour of sky.
 - (a) Black
- (b) Water
- (c) White
- (d) Blue

A115.	(6)				
57.	Which of the following can be formed from "RECCOMMENDATION" word letters				
	(a) MEDIATE	(b) COMMUNICA	ΓE (c) MEDICINE	(d) REMAINDER	
Ans.	(a)				
58.	•	gful words can be formed with the first, the third, the seventh and the ninth letters of the wing each letter only once in each word?			e word
	(a) 3	(b) 4	(c) more than 4	(d) 2	
Ans.	(c)				
59.	Find a number from	n the given options which	best completes the ser	ies: 39, 416, 525,, 749, 864	•
	(a) 439	(b) 436	(c) 636	(d) 644	
Ans.	(c)				
60.	-	work in 10 days and B ca in 2 days. In how many		after 4 days B left and C joins ther rk	n A and
	(a) 12 days	(b) 15 days	(c) 10 days	(d) 20 days	
Ans.	(c)				
61.	1. Thirty-six vehicles are parked in a parking lot in a single row. After the first car, there is one scooter second car, there are two scooters. After the third car, there are three scooters and so on. Wor number of scooter in the second half row.				
	(a) 15	(b) 17	(c) 12	(d) 10	
Ans.	(a)				
62.	Deepa moved a distance of 75 metre towards the north. She then turned left and walking for about 25 met turned left again and waked 80 meters. Finally, she turned to the right at an angle of 45°. In which direction we she moving finally?				
	(a) North – East	(b) North – West	(c) South – East	(d) South – West	
Ans.	(d)				
63.		of milk and water 10% we in the mixture comes do		nould be added so that the percen	tage of
	(a) 120	(b) 80	(c) 90	(d) 60	
Ans.	(a)				
64.	Rakesh says to Mahesh – "I am as old as you were when I was one-third as you are". If the sum of their ages is 60 year, find the present age of the Mahesh (in years).				
	(a) 45	(b) 36	(c) 30	(d) 24	
Ans.	(b)				
65.	Hari invested an amount at a certain rate of interest on simple interest and he got 60% more amount after 8 years. If he invest Rs. 9600 at the same rate of interest on simple interest then find total interest he would get after four years.				

(c) Rs. 2880 (d) Rs. 2160

(a) Rs. 2520 (b) Rs. 2260

Ans.	(c)					
66.	Ritu purchased 20 dozen of Banana at the rate of Rs. 375 per dozen. She sold each one of them at the rate Rs. 33. What was the percentage profit.					
	(a) 12.3%	(b) 5.6%	(c) 6.5%	(d) 10%		
Ans.	(b)					
67.	Auniversity is offering elective courses in Mathematics, Economics and Sociology. Each of its 100 ur students has to opt for at least one of these electives. Course enrollment data showed that 47 students for Mathematics, 47 students enrolled for Economics and 57 students enrolled for Sociology. I enrolled for all three courses, how many students enrolled for exactly one course?					
	(a) 60	(b) 56	(c) 58	(d) Cann't say		
Ans.	(b)					
68.		• •		ni and Sweta are four sister. Pounger than rakhi, then who is		
	(a) Sweta	(b) Yamini	(c) Pooja	(d) Rakhi		
Ans.	(b)					
	Conclusion: I. Some tea II. Some str	ome boys are students. acher are students. udents are boys. I follows (b) Neither I n	or II follows (c) Only II	follows (d) Only I follows		
Ans.	(d)					
70.	Identify the next two numbers in the following sequence: 17, 20, 9, 12, 5, 6, 3, 2, ?, ?					
	(a)(0,2)	(b)(1,2)	(c)(2,0)	(d)(2,1)		
Ans.	(c)					
71.	Study the diagram	m and answer the question	on that follows:			
		Player	15 Girl 16 30 14 18 17 12	Coach		
	(a) 16	(b) 31	(c) 15	(d) 61		
Ans.	(a)					
72.	Three persons A, B and C are standing in queue. There are five persons between A and B and eight persons					

number of persons in the queue?

(b) 27

(a) 40

(c)

Ans.

(c) 28

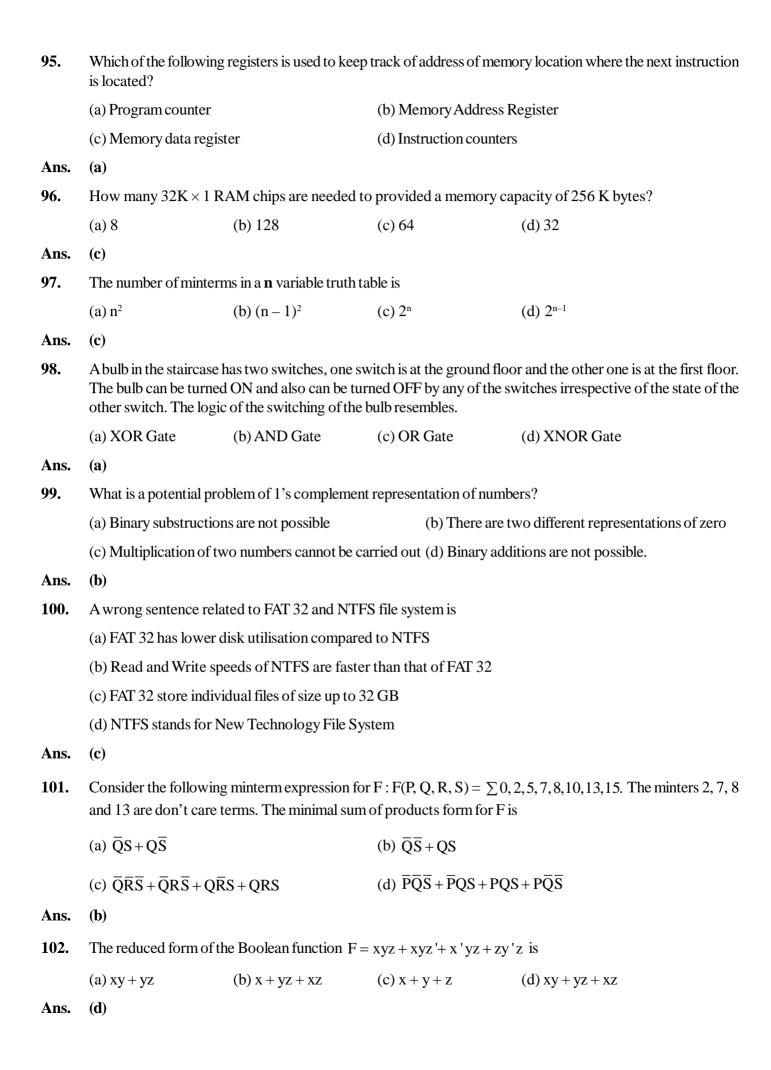
between B and C. If there are three persons ahead of C and 21 behind A, then what could be the minimum

(d)41

73.	Hemant deposits 10% of his salary in PF. He saves 30% of remaining salary. The ratio of his expenses on medicine and groceries is 3:4 of remaining salary after saving. If his expenses in medicine was Rs. 2700, then find his monthly salary.				
	(a) Rs. 30,000	(b) Rs. 20,000	(c) Rs. 10,000	(d) Rs. 15,000	
Ans.	(c)				
74.			*	ngth same as that of the train in 36 sec. a in 25 sec, then find speed of Duranto	
	(a) 54 km/h	(b) 72 km/h	(c) 84 km/h	(d) 90 km/hr	
Ans.	(b)				
75.	If 20 – 10 means 200,	$8 \div 4 \text{ mean } 12, 6 \times 2 \text{ m}$	neans 4 then $\lceil (100-10) \rceil$	$\times (1000 \div 1000) + (100 \times 10) =$	
	(a) 20	(b) 0	(c) 1090	(d) None of these	
Ans.	(b)				
76.	If DENMARK in code	ed on FCPKCPM Then	code SINGAPORE of	which option.	
	(a) UGPECNQPG	(b) UGPFCNRPG	(c) UGPEDNQTC	(d) UGPECNQTC	
Ans.	(a)				
77.	In the given word "LAVISHLY" if all the consonants replaced with its previous letter and all the vowels replaced with its next letter after that remove all the repeated letter and arranged them in alphabetical order then, which of the following letters is 3rd from the left end				
	(a) R	(b) U	(c) J	(d) G	
Ans.	(c)				
78.	students are passed in		naining students (who fa	hese (passed in half-yearly) only 70% ail in half-yearly exam) 80% passed in	
	(a) 76%	(b) 72%	(c) 74%	(d) 65%	
Ans.	(c)				
79.	Arrange in correct ord	er			
	(1) Database	(2) Analysis (3) Su	rvery (4) Policy form	nation (5) Interpretation	
	(a) 2, 1, 5, 3, 4	(b) 5, 4, 3, 1, 2	(c) 3, 1, 2, 4, 5	(d) 3, 1, 2, 5, 4	
Ans.	(d)				
80.	Two friends A and B were standing at the diagonally opposite corners of a rectangular plot whose perimeter is 100m. A first walked x meters along the length of the plot towards East and then y meters towards the South. B walked x meters along the breadth towards North and then y meters towards West. At the end of their walks, A and B were standing at the diagonally opposite corners of a smaller rectangular plot whose perimeter is 40m. How much distance did A walk?				
	(a) 15	(b) 40	(c) 25	(d) 50	
Ans.	(a)				

81.	On Monday, Akash run 4 km less than the distance he ran on Tuesday. Sanjay, who ran the same distance on Monday and Tuesday, ran 5 km more on Tuesday than the distance Akash ran on Monday. Find the difference between the distance covered by Akash and Sanjay over the two days.				
	(a) 5 km	(b) 6 km	(c) 4 km	(d) 9 km	
Ans.	(b)				
82. 1.	Statement: No table is chair. Not a single chair is statue. Ever stand is statue. Conclusion: Some statue which are	and. e stand are table as well.			
2.	Some statue are not ch				
	(a) If neither conclusion(c) Only conclusion 2 to		(b) If only conclusion (d) None of these	1 follows	
Ans.	(c)				
83.	If the word IMPACT DESCEND?	is coded as RNKZXG,	then which of the follow	ving represents the code for the word	
	(a) WVHXVMW	(b) MNBLNWM	(c) MFBDFOM	(d) MFBDNOM	
Ans.	(a)				
84. ⇒ ⇒ ⇒ ⇒ ⇒	A junior school is offering five after-school activities - Karate, Handwork, Music Dance and Gymnastics. Each of the five students – Leena, Megan, Neha, Omar and Pixia has subscrived to at least one activity. As per the school rules, anyone who subscribes to Gymnastics must also subscribe to Dance. Karate and Handwork must always be subscribed together. Music and Dance cannot be subscribed together. The following information is available about the student's subscriptions. Megan subscribed to four activities. Leena subscribed to Gymnastics but not Karate. Pixie subscribed to only one activity and is the only one subscribe to that activity. Omar subscribed to three activities. Neha subscribed to only one activity. How many activities are subscribed by exactly two people each?				
Ans.	(d)				
85.	If 'E' stands for +, 'F'	'stands for '-', 'M' sta	nds for 'x', 'N' stands f	For \div , then 19 M 5 E 39 N 3 F 8 = ?	
	(a) 105	(b) 100	(c) 95	(d) 90	
Ans.	(b)				
86.	In a reality show, two judges independently provided marks based on the performance of the participants. If the marks provided by the second judge are given by $y = 1 + x$, where x is the marks provided by the first judge. Then for a participant (a) Ranks given by both the judge differ by 2 (b) Rank given by the second judge is more than that of the first judge (c) Ranks given by both the judges are same. (d) Rank given by the first judge is more than that of the second judge				
Ans.	(c)				

87.	Fill the blanks with the most appropriate combination of options.					
	_	- · ·	-	ncouraged to exiting to duly shore up floating		
	(a) affect, negotiate	(b) abandon, imply	(c) precaution, abstra	act (d) reissue, stocks		
Ans.	(d)					
88.		nd 18 litres water added		5: 4 respectively P litre of mixture taken ure, then the new ratio of milk to water		
	(a) 57	(b) 19	(c) 27.5	(d) 38		
Ans.	(d)					
89.	•	a bank manager decided 7, then 52191 is coded	* *	number in the server. If A/C No. 46873		
	(a) 4108041	(b) 5219152	(c) 1153193	(d) 1043293		
Ans.	(c)					
90.				ers and then the position of the digits are er after they are arranged in descending		
	589 362 554 371 44	589 362 554 371 442				
	(a) 3	(b) 2	(c) 4	(d) 1		
Ans.	(a)					
		Co	<u>mputer</u>			
91.	The maximum and minimum value represented in signed 16 bit 2's complement representations are					
	(a) -16684 and 1638	33 (b) 0 and 32767	(c) 0 and 65535	(d) –32678 and 32767		
Ans.	(d)					
92.	The time required for	fetching & execution on	e machine instruction is			
	(a) Delay time	(b) CPU cycle	(c) Real time	(d) Seek time		
Ans.	(b)					
93.	Consider the circuit sl	hown below and find mi	nimum number of NAN	D gates required to design it.		
	A	Y				
	(a) 4	(b) 6	(c) 3	(d) 5		
Ans.	(a)					
94.	If a processor clock is	s rated as 2500 million c	cycles per seconds, ther	n its clock period is		
	(a) 2.50×10^{-10} sec	(b) $4.0 \times 10^{-10} \text{sec}$	(c) $1.0 \times 10^{-10} \text{sec}$	(d) $5.0 \times 10^{-10} sec$		
Ans.	(b)					



103.	Suppose we have a 10-bit computer that uses 10-bit into (2's complement representation). The number representation of -35 is				
	(a) 0000100011	(b) 1100100011	(c) 1111011101	(d) 1111011101	
Ans.	(c)				
104.	Consider the following products form of F is	g Boolean expression fo	r F: F(P, Q, R, S) = PQ	$+\overline{P}QR + \overline{P}Q\overline{R}S$. The minimum sum of	
	(a) $PQ + QR + QS$	(b) $P + Q + R + S$	(c) $\overline{P} + \overline{Q} + \overline{R} + \overline{S}$	(d) $\overline{P}R + \overline{P}\overline{R}S + P$	
Ans.	(a)				
105.	What is the name of the to another?	e storage device that cor	mpensates the difference	in rates of flow of data from one device	
	(a) Cache	(b) Buffer	(c) Concentrator	(d) RAM	
Ans.	(b)				
106.	Equavalent of the deci	imal number $(25.375)_{10}$	in binary form		
	(a) $(11001.011)_{10}$	(b) $(11101.011)_{10}$	(c) $(11011.111)_{10}$	(d) $(11001.101)_{10}$	
Ans.	(a)				
107.	•		1 0	processor has a translation look-aside way set associative. The minimum size	
	(a) 13 bits	(b) 20 bits	(c) 11 bits	(d) 15 bits	
Ans.	(d)				
108.	(a) It has separate stor(b) It has a separate pr(c) It has separate men	g is true about Von New rage for input/output operocessing unit for data and mory for data and instrumory unit for both data and	erations nd instructions ctions		
Ans.	(d)				
109.	Let \oplus and \odot denote the Exclusive – OR and Exclusive – NOR operations respectively. Which one of the following is not correct?				
	(a) $\overline{P} \oplus \overline{Q} = P \odot Q$	(b) $\overline{P} \oplus Q = P \odot Q$	(c) $\overline{P} \oplus \overline{Q} = P \oplus Q$	(d) $(P \oplus \overline{P}) \oplus Q = (P \odot \overline{P}) \odot \overline{Q}$	
Ans.	(d)				
110.	Suppose we have a 10-bit computer that uses 10-bit floating point computational unit (Flot number uses IEEE floating-point arithmetic where a floating point number has 1 sign bit, 5 exponent bits, and 4 fraction bits). The representation for $+\infty$ (plus infinity) is				
	(a) 0 11111 0000	(b) 1 11111 0000	(c) 0 00000 1111	(d) 0 11111 1111	
Ans.	(a)				

English

111. Comprehension:

Science and religion – the two terms have come to signify a mutual antagonism. The two, it is commonly declared, are poles apart; their spheres of activity and their methods differ widely, so much so that they are considered to be irreconcilable.

On the face of it, science and religion appear to be the two opposite poles of man's consciousness. Science is basically concerned with the material world; its efforts are directed towards unraveling the "how" of reality while religion is concerned with the "why" of reality. Science deals with analyzing tangible entities into its minutest parts, and then arrives at conclusions about the way in which tangible realities are organized. While science is analytical, religion takes the ultimate reality for granted. Religion follows the metaphysical path; the concept of God is ultimately a matter of faith and it is this faith which is the basis of the religious man's attribution of a design or meaning for the reality.

The modes of action are different in science and religion. Science relies on experiment, whereas religion is based on experience. Any religious experience, whether it is Christ's or Ramakrishna's, is personal and subjective. Science, on the other hand, is marked by objectivity. Theory has to be corroborated by tangible proof. Science benefits mankind by providing material comforts. The frontiers of science do not end in knowledge but are extended to the formation of appliances for actual use. Science, it has been somewhat unfairly charged, cultivates the materialistic thinking. However, it has to be admitted that the mental attitude promoted by religion is entirely different, while the basis of scientific progress is unbridled curiosity and courageous endeavour, the truly religious spirit cavils at such presumption that man's mind can penetrate the mysteries of the universe. Science promotes fearless inquiry while an essential ingredient of religion is the humility born of fear of God. Science incorporates a love of experimental knowledge, while religion does not believe in the rational approach.

Which of the following statements according to the passage is correct:

- (a) The religious spirit assumes that human mind can penetrate the mysteries of the universe.
- (b) Science follows the metaphysical path.
- (c) Science believes in the humility born of fear of God.
- (d) Religion believes in ultimate reality

Ans. (d)

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	a love of experimen	tal knowledge, while religi	on does not believe in	the rational approach.		
Q.	Which of the followscience?	wing reasons according to	the passage provide	material comforts to people in case of		
	(a) Trangible proofs	s of the theories of science	(b) Materialistic thin	king being cultivated by science		
	(c) Promotion of fe	arless inquiry by science	(d) The subjectivity	of science		
Ans.	(a)					
113.	Select the most app	ropriate meaning of the unc	derlined idiom in the gi	ven sentence:		
	Off and on, I take a	break from my hectic sche	edule to refresh myself			
	(a) Periodically	(b) Rarely	(c) Seldom	(d) Immediately		
Ans.	(a)					
114.	I have u	mbrella. I bought it	year ago.			
	(a) A, An	(b) An, A	(c) An, The	(d) Then, An		
Ans.	(b)					
115.	Synonym for "Nong (a) Flummoxed	plussed" is (b) Dumbfounded	(c) Befuddled	(d) Oriented		
Ans.	(d)					
116.		ropriate preposition to fill ineone who look (b) for		en. (d) over		
Ans.	(a)	(0)101	(6) 611	(a) 5 voi		
117.	, ,	ropriate preposition to fill i	n the blank.			
	We haven't been to Delhi almost five years.					
		(b) since		(d) for		
Ans.	(d)					
118.	Meaning of "Abrog	ate" is				
	(a) Abolish	(b) Absorb	(c) Abstract	(d) Ablaze		
Ans.	(a)	. ,	` ,	,		
119. Ans.	Choose the best option that indicates the change of voice for the sentence given below: They sent for a doctor because Pamela had fainted (a) Pamela fainted and a doctor was sent for (b) A doctor was sent for them because Pamela has fainted (c) A doctor was sent for because Pamela had fainted (d) Pamela had sent for a doctor because they had fainted (c)					

120. Antonym for "Spendthrift" is

(a) Profligate

(b) Extravagant

(c) Frugal

(d) Squanderer

Ans. (c)